

# A Di Perna-Lions Theory on Wiener Spaces

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In [DL89], R.J. DiPerna and P.-L. Lions first proved that Sobolev regularity for vector fields in  $\mathbb{R}^n$  (with bounded divergence) is sufficient to establish existence, uniqueness and stability of a generalized notion of flow, consisting of a suitable selection among the trajectories of the associated ODE: later on, the important case of  $BV$  fields was settled by L. Ambrosio, in [Amb04].

In this seminar we will introduce and motivate the infinite dimensional counterparts of these results, in the setting of abstract Wiener spaces, as developed in [AF09] (Sobolev fields) and in [Tre13] ( $BV$  fields).

## References

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